#### **NS7-56 Fraction and Decimal Patterns**

A **unit fraction** has 1 in the numerator. Examples:  $\frac{1}{2}$ ,  $\frac{1}{3}$ ,  $\frac{1}{7}$ 

1. Write the fraction as a sum of unit fractions and as a product of a fraction and a whole number.

a) 
$$\frac{3}{8} = \frac{1}{8} + \frac{1}{8} + \frac{1}{8} = \dots \times \frac{1}{8}$$
 b)  $\frac{3}{4} =$ 

b) 
$$\frac{3}{4}$$
 =

c) 
$$\frac{4}{5}$$
 =

2. Write the fraction as a sum of unit fractions. Then write the unit fractions as

a) 
$$\frac{3}{5} = \frac{1}{5} + \frac{1}{5} + \frac{1}{5} = 0.2 + 0.2 + 0.2 = 0.6$$

b) 
$$\frac{4}{5}$$
 =

c) 
$$\frac{3}{4}$$
 =

d) 
$$\frac{3}{2}$$
 =

3. Write the fraction as the product of a unit fraction and a whole number. Then write the unit fraction as a decimal and multiply.

a) 
$$\frac{4}{5} = 4 \times \frac{1}{5} = 4 \times 0.2 = 0.8$$

b) 
$$\frac{3}{4}$$
 =

c) 
$$\frac{3}{5}$$
 =

d) 
$$\frac{5}{4}$$
 =

- 4. a) What is the rule for the pattern 0.05, 0.10, 0.15, 0.20, ...?
  - b)  $\frac{1}{20} = 0.05$ ,  $\frac{2}{20} = 0.10$ ,  $\frac{3}{20} = 0.15$ ,...Continue the pattern to write  $\frac{11}{20}$  as a decimal.
  - c) If you know  $\frac{1}{20} = 0.05$ , how can you use multiplication to find  $\frac{11}{20}$  as a decimal?
- 5. a)  $\frac{1}{4} = 0.25$ , so  $\frac{7}{4} = \underline{7} \times \underline{0.25}$  b)  $\frac{1}{5} = 0.$ , so  $\frac{21}{5} = \underline{\phantom{0}} \times \underline{\phantom{0}}$  c)  $\frac{1}{2} = 0.$ , so  $\frac{13}{2} = \underline{\phantom{0}} \times \underline{\phantom{0}}$ = 1.75
  - 6. Write the fractions as decimals. Add the decimals. Write the sum as a fraction in lowest terms. Check your answer by adding the fractions.

a) 
$$\frac{1}{4} + \frac{2}{5} = 0.25 + 0.4 = 0.65 = \frac{65}{100} = \frac{13}{20}$$

b) 
$$\frac{1}{2} + \frac{1}{5}$$

Check: 
$$\frac{5 \times 1}{5 \times 4} + \frac{2 \times 4}{5 \times 4} = \frac{5}{20} + \frac{8}{20} = \frac{13}{20}$$

c) 
$$\frac{1}{2} + \frac{4}{5}$$

d) 
$$\frac{3}{2} + \frac{3}{4}$$

## NS7-57 Relating Fractions and Division



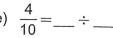
 $\frac{1}{2}$  is one whole divided into 2 parts, so  $\frac{1}{2} = 1 \div 2$ .

- 1. a)  $\frac{1}{4} = 1 \div$
- b)  $\frac{1}{3} = \div$

- **2.** a) Explain why  $24 \div 2$  is three times  $8 \div 2$ .
- b) Explain why  $3 \div 8$  is three times  $1 \div 8$ .

c) Explain why  $3 \div 8$  is  $3 \times \frac{1}{6}$ .

- d) Explain why  $3 \div 8 = \frac{3}{6}$ .
- 3. Use  $\frac{a}{b} = a \div b$  to write the fraction as a decimal. Keep dividing until the remainder is 0.
- a)  $\frac{1}{5} = 1 \div 5$  b)  $\frac{2}{5} = \underline{\phantom{0}} \div \underline{\phantom{0}}$  c)  $\frac{3}{6} = \underline{\phantom{0}} \div \underline{\phantom{0}}$  d)  $\frac{1}{2} = \underline{\phantom{0}} \div \underline{\phantom{0}}$  e)  $\frac{4}{10} = \underline{\phantom{0}} \div \underline{\phantom{0}}$

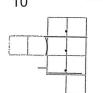












So, 
$$\frac{1}{5} = 0$$
. So,  $\frac{2}{5} = 0$ . So,  $\frac{3}{6} = 0$ . So,  $\frac{1}{2} = 0$ . So,  $\frac{4}{10} = 0$ .

So, 
$$\frac{2}{5} = 0$$
.\_\_\_

So, 
$$\frac{3}{6} = 0$$
.\_\_\_

So, 
$$\frac{1}{2} = 0$$
.\_\_\_

So, 
$$\frac{4}{10} = 0$$
.\_\_\_

- h)  $\frac{7}{10}$  i)  $\frac{3}{5}$
- j)  $\frac{12}{30}$
- 4. a) Change the fraction to a decimal using long division. Keep dividing until the remainder is 0,

$$\frac{1}{8} = 8\overline{)1.000} = ?$$

$$\frac{2}{8} = 8\overline{)2.000} = ?$$

$$\frac{3}{8} = 8\overline{)3.000} = ?$$

- b) What is the pattern in the decimal equivalents in part a)?
- c) Extend the pattern from part a) to predict the decimals equivalent to  $\frac{4}{8}$ ,  $\frac{5}{8}$ ,  $\frac{6}{8}$ ,  $\frac{7}{8}$ , and  $\frac{8}{8}$ .
- 5. Convert each fraction to a decimal fraction. Then change the fraction to a decimal. Check your answers using a calculator.

a) 
$$\frac{3}{40} = \frac{75}{1000} = 0.075$$

b) 
$$\frac{17}{20} = \frac{1}{100}$$

c) 
$$\frac{19}{125} = \frac{1000}{1000}$$

Check: 
$$3 \div 40 = 0.075$$

d) 
$$\frac{13}{25}$$

e) 
$$\frac{3}{5}$$

f) 
$$\frac{351}{500}$$

g) 
$$\frac{39}{200}$$

BONUS ▶ 
$$\frac{5}{16}$$

## NS7-63 Writing Repeating Decimals as Fractions (Advanced)

a) 
$$0.\overline{7} = \frac{1}{9}$$

b) 
$$0.\overline{23} = \frac{1}{99}$$

c) 
$$0.\overline{05} = \frac{1}{99}$$

a) 
$$0.\overline{7} = \frac{1}{9}$$
 b)  $0.\overline{23} = \frac{1}{99}$  c)  $0.\overline{05} = \frac{1}{99}$  d)  $0.\overline{441} = \frac{1}{999}$  e)  $0.\overline{652} = \frac{1}{999}$ 

e) 
$$0.\overline{652} = \frac{}{999}$$

f) 
$$0.\overline{98} =$$

g) 
$$0.\overline{5} =$$

h) 
$$0.\overline{461} =$$

i) 
$$0.\overline{38} =$$

f) 
$$0.\overline{98} =$$
 g)  $0.\overline{5} =$  h)  $0.\overline{461} =$  i)  $0.\overline{38} =$  j)  $0.\overline{061} =$ 

#### 2. Multiply or divide by moving the decimal point the correct number of places, left or right.

d) 
$$0.\overline{32} \times 100$$

e) 
$$0.3\overline{2} \div 100^{\circ}$$

g) 
$$0.3\overline{41} \div 10$$

h) 
$$7.4\overline{32} \div 1000$$

3. a) 
$$\frac{1}{9} = \underbrace{0.111...}$$
 b)  $\frac{4}{9} = \underbrace{-----}$ 

b) 
$$\frac{4}{9} =$$
\_\_\_\_\_

c) 
$$\frac{2}{3} =$$
\_\_\_\_\_

So 
$$\frac{1}{90} = 0.0111...$$

So 
$$\frac{4}{900}$$
 = \_\_\_\_\_

4. 
$$\frac{137}{999} = 0.\overline{137}$$
. What is  $\frac{137}{9990}$ ?

**5.** a) 
$$13 \times 0.01 =$$
 \_\_\_\_\_\_

$$13 \times 0.0111 =$$

c) Why should 
$$\frac{13}{90}$$
 be equal to your answer to part b)? Check using a calculator.

d) Use 
$$\frac{13}{9} = 1\frac{4}{9}$$
 to find  $\frac{13}{90}$  in a different way.

#### 6. Write each decimal as a fraction.

a) 
$$0.\overline{1} = \underline{\qquad} 0.\overline{8} = \underline{\qquad} 0.0\overline{8} = \underline{\qquad} 0.0\overline{27} = \underline{\qquad$$

$$0.\overline{1} = \underline{\qquad} 0.\overline{8} = \underline{\qquad} 0.0\overline{8} = \underline{\qquad} 0.0\overline{1} = \underline{\qquad} 0.\overline{01} = \underline{\qquad} 0.0\overline{27} = \underline{\qquad} 0.0\overline{27} = \underline{\qquad} 0.5\overline{8} = 0.5 + 0.0\overline{8} = \underline{\qquad} + \underline{\qquad} = \underline{\qquad} 0.4\overline{27} = 0.4 + 0.0\overline{27} = \underline{\qquad} + \underline{\qquad} = \underline{\qquad}$$

c) 
$$0.\overline{001} = \underline{\phantom{0}} 0.\overline{253} = \underline{\phantom{0}} 0.0\overline{253} = \underline{\phantom{0}} 0.0\overline{5} = \underline{\phantom{0}} \text{ so } 4.\overline{5} = \underline{\phantom{0}}$$
  
 $5.6\overline{253} = \underline{\phantom{0}} + \underline{\phantom{0}} = \underline{\phantom{0}} + \underline{\phantom{0}} = \underline{\phantom{0}} 0.0\overline{5} = \underline{\phantom{0}} \text{ so } 4.0\overline{5} = \underline{\phantom{0}}$ 

f) 
$$1.\overline{7}$$
 g)  $2.\overline{35}$  h)  $0.24\overline{361}$  i)  $2.4\overline{361}$ 

#### NS7-64 Percents

The words "per cent" mean "out of 100." A percent is a ratio that compares a number or amount to 100.

The symbol for percent is %. Example: 45% = 45:  $100 = \frac{45}{100}$ 

1. a) 30 out of 100 squares are shaded. The ratio of shaded squares to all squares is \_\_\_\_: 100.

So, \_\_\_\_% of the grid is shaded.



b) 47 out of 100 letters are Bs. The ratio of Bs to all letters in the set is \_\_\_\_: 100.

So, \_\_\_\_% of the letters are Bs.

**ABBBCCBBAABBCABBBCCB** AAABBBCCBBAABAAABBBC **CBCABBBCCBBBCCBBAAAB** BAAABBABCBBAABCCBBAB **BCCBAABBAAAABBCCABAA** 

2. Write the ratio as a percent.

a) 20:100 = \_\_\_\_% b) 63:100 = \_\_\_\_% c) 5:100 = \_\_\_\_% d) 55:100 = \_\_\_\_%

Write the percent as a ratio.

a) 30% = \_\_\_\_: <u>100</u> b) 12% = \_\_\_\_: \_\_\_ c) 25% = \_\_\_\_: \_\_\_ d) 34% = \_\_\_\_:

4. Write the ratio as a fraction and as a percent.

a)  $50:100 = \frac{100}{100} = \frac{\%}{100}$ 

b)  $10:100 = \frac{100}{100} = \frac{100}{100}$ 

5. Write the fraction as a percent.

a)  $\frac{40}{100} =$  \_\_\_\_% b)  $\frac{28}{100} =$  \_\_\_\_% c)  $\frac{43}{100} =$  d)  $\frac{1}{100} =$  e)  $\frac{10}{100} =$ 

6. Write the percent as a fraction.

a)  $11\% = \frac{100}{100}$  b)  $89\% = \frac{100}{100}$  c) 9% = d) 75% = e) 100% =

7. Complete the chart.

Drawing				2. 169 2. 168
Fraction	23 100	100	45 100	100
Percent	23%	63%	%	%

### NS7-65 Adding and Subtracting Percents

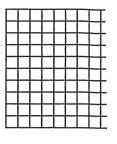
1. There are 100 squares on the grid.

Colour 10 out of 100 squares red. The red area is \_\_\_\_% of the grid.

Colour 40 out of 100 squares blue. The blue area is \_\_\_\_% of the grid.

There are now 10 + 40 =\_\_\_ coloured squares on the grid.

So, % of the grid is coloured.



2. Write the percents as fractions. Add or subtract. Then write the sum or difference as a percent.

a) 
$$30\% + 20\% = \frac{100}{100} + \frac{100}{100} = \frac{100}{100} = \frac{100}{100}$$

a) 
$$30\% + 20\% = \frac{1}{100} + \frac{1}{100} = \frac{1}{100} = \frac{1}{100}\%$$
 b)  $10\% + 50\% = \frac{1}{100} + \frac{1}{100} = \frac{1}{100}\%$ 

c) 
$$50\% - 25\% = \frac{100}{100} - \frac{100}{100} = \frac{100}{100} = \frac{100}{100}$$

c) 
$$50\% - 25\% = \frac{100}{100} - \frac{100}{100} = \frac{100}{100} =$$

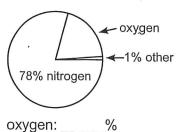
3. Calculate.

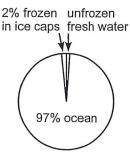
a) 
$$12\% + 20\% =$$
\_\_\_% b)  $33\% + 44\% =$ %

b) 
$$33\% + 44\% = ____\%$$

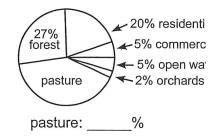
c) 
$$56\% - 23\% + 8\% = \%$$

- 4. Determine the missing percent in the circle graph. The whole circle represents 100%.
  - a) Gases in Earth's Atmosphere b) Composition of Earth's Water





c) Land Cover in North America



unfrozen fresh water: %

5. a) The ratio of cents in a penny to cents in a dollar is 1:100, so a penny is % of a dollar.

The ratio of cents in a dime to cents in a dollar is \_\_\_\_ : 100, so a dime is \_\_\_\_% of a dollar.

A quarter is \_\_\_\_ cents out of 100, so a quarter is \_\_\_\_% of a dollar.

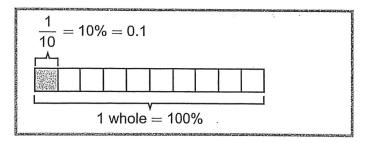
b) What percent of a dollar is 35 cents? \_\_\_\_%

What percent of a dollar is two pennies and two quarters? %

c) You have a dollar and you spend 26¢. What percent of the dollar do you have left? \_\_\_\_%

#### NS7-66 Tenths, Decimals, and Percents

- 1. Shade the percent.
  - a) 50%
  - b) 30%



**2.** \_\_\_\_% of the 10 dots are white.





3. a) Shade 80% of the 10 dots.

b) What percent of the dots are not shaded?



- 4. 10% of 100 marbles are blue. How many of the marbles are not blue? \_\_\_\_\_
- 5. Write the percent as a fraction and then as a decimal.

a) 
$$90\% = --- = 0$$
.

b) 
$$35\% = \frac{100}{100} = 0.$$

c) 
$$22\% = \frac{100}{100} = 0$$
.

a) 
$$90\% = \frac{100}{100} = 0$$
. b)  $35\% = \frac{100}{100} = 0$ . c)  $22\% = \frac{100}{100} = 0$ . d)  $6\% = \frac{100}{100} = 0$ .

6. Write the percent as a decimal.

7. Write the decimal as a percent.

a) 
$$0.2 = \frac{2}{10} = \frac{2}{100} = \frac{2}{100$$

b) 
$$0.3 = \frac{10}{100} = \frac{9}{100}$$

d) 
$$0.23 = \frac{100}{100} = \frac{\%}{100}$$
 e)  $0.57 = \frac{\%}{100}$ 

8. Write the decimal as a percent by moving the decimal point two places to the right.

a) 
$$0.4 = _{--}\%$$

a) 
$$0.4 = ____\%$$
 b)  $0.6 = ____\%$  c)  $0.3 =$ 

c) 
$$0.3 =$$

d) 
$$0.1 =$$

f) 
$$0.72 = ____%$$
 g)  $0.20 = ____%$  h)  $0.45 =$  i)  $0.06 =$ 

**9.** Approximately what percent does the decimal represent? Example:  $0.1234 \approx 0.12 = 12\%$ . Hint: Remember to round to two decimal places.

a) 
$$0.382 \approx$$
\_\_\_\_%

c) 
$$0.3779 \approx$$

10. Kay bought 6 jazz CDs and 4 rock CDs. What fraction of the CDs are jazz? What percent are rock?

JUMP MATH: NOT TO BE COPIED

## 187-67 Fractions and Percents

Write the fraction as a percent by changing it to a fraction over 100.

a) 
$$\frac{3 \times 20}{5 \times 20} = \frac{60}{100} = 60\%$$

b) 
$$\frac{4}{5}$$

c) 
$$\frac{3}{20}$$

d) 
$$\frac{8}{25}$$

- 2. Two out of five friends, or  $\frac{2}{5}$ , ordered pizza. What percent ordered pizza?
- 3. Change the fraction to a percent. Reduce the fraction to lowest terms if necessary.

a) 
$$\frac{9}{15} = \frac{3}{5} = \frac{60}{100} = 60\%$$

b) 
$$\frac{3}{15}$$
=

c) 
$$\frac{9}{18}$$
 =

d) 
$$\frac{6}{24}$$
 =

e) 
$$\frac{3}{4}$$

f) 
$$\frac{1}{2}$$

g) 
$$\frac{4}{10}$$

(h) 
$$\frac{18}{25}$$

$$\frac{28}{40}$$

4. Divide to change the fraction to a decimal. Then write the decimal as a percent.

a) 
$$\frac{3}{4} = 3 \div 4 = 0$$
. \_\_\_ = \_\_\_% b)  $\frac{4}{5}$  c)  $\frac{3}{15}$  d)  $\frac{15}{25}$ 

b) 
$$\frac{4}{5}$$

c) 
$$\frac{3}{15}$$

d) 
$$\frac{15}{25}$$

e) 
$$\frac{65}{500}$$

5. Write the percent as a decimal, then as a fraction, then in lowest terms.

**6.** Is the fraction closest to 10%, 25%, 50%, 75%, or 100%?

a) 
$$\frac{4}{5}$$

b) 
$$\frac{2}{10}$$

c) 
$$\frac{2}{5}$$

a) 
$$\frac{4}{5}$$
 b)  $\frac{2}{10}$  c)  $\frac{2}{5}$  d)  $\frac{9}{10}$  e)  $\frac{11}{20}$ 

e) 
$$\frac{11}{20}$$

f) 
$$\frac{16}{20}$$

g) 
$$\frac{4}{25}$$

7. Estimate what percent the fraction is. Say what fraction you used to make your estimate. Then divide to change the fraction to a decimal. Was your estimate close?

a) 
$$\frac{11}{40}$$

b) 
$$\frac{23}{49}$$

c) 
$$\frac{60}{84}$$

d) 
$$\frac{14}{24}$$

e) 
$$\frac{4}{42}$$

f) 
$$\frac{21}{31}$$

8. Write the fraction as a decimal. Round to two decimal places. Write the approximate percent.

a) 
$$\frac{5}{12} = 5 \div 12 = 0.41\overline{6} \approx 0.42 =$$
 b)  $\frac{1}{3}$  c)  $\frac{2}{3}$  d)  $\frac{2}{9}$  e)  $\frac{5}{6}$  f)  $\frac{1}{7}$ 

b) 
$$\frac{1}{3}$$

c) 
$$\frac{2}{3}$$

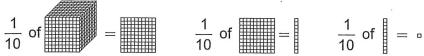
d) 
$$\frac{2}{9}$$

$$\Rightarrow$$
)  $\frac{5}{6}$ 

f) 
$$\frac{1}{7}$$

### **NS7-70 Finding Percents**

If you use a thousands cube to represent 1 whole, you can see that taking  $\frac{1}{10}$  of a number is the same as dividing by 10 (the decimal shifts one place left):



$$\frac{1}{10}$$
 of  $=$ 

$$\frac{1}{10}$$
 of  $=$ 

$$\frac{1}{10}$$
 of  $1 = 0.1$ 

$$\frac{1}{10}$$
 of  $0.1 = 0.01$ 

$$\frac{1}{10}$$
 of 0.1 = 0.01  $\frac{1}{10}$  of 0.01 = 0.001

- 1. Find  $\frac{1}{10}$  of each number by shifting the decimal. Write your answers in the boxes provided.

- d) 210
- e) 6.4
- f) 50.6

- 2. 10% is short for  $\frac{10}{100}$  or  $\frac{1}{10}$ . Find 10% of each number.
  - a) 1
- b) 3.9
- c) 4.05
- d) 6.74
- e) 0.09
- f) 60.08

#### How to Find Percents That Are Multiples of 10

Step 1: Find 10% of the number.

Step 2: Multiply the result by the number of tens in the percent.

Example: Find 30% of 21.

There are 3 tens in 30 (30 =  $3 \times 10$ ).

$$3 \times 2.1 = 6.3$$

So 30% of 
$$21 = 6.3$$
.

- 3. Find the percent using the method above.
  - a) 30% of 15

d) 40% of 75

e) 90% of 86

f) 80% of 0.5

**4.** If you know 10% of a number *n*, then 5% of *n* is 10% divided by 2. Complete the chart.

5%	3			
10%	6	20	42	1
100%	60			

Use these steps to find 1% of a number:

**Step 1:** Change the percent to a decimal and replace "of" with "x."

**Step 2:** Multiply by 0.01 by shifting the decimal two places left.

5. Fill in the blanks.

a) 1% of 300 = 
$$0.01 \times 300 =$$

6. Find 1% of 200 and use your answer to calculate each percent.

7. Use the method of Question 6 to calculate...

- a) 4% of 800
- b) 2% of 50
- c) 11% of 60 d) 2% of 4 e) 7% of 45

**8.** Fill in the missing numbers. (Hint: 8% = 4% + 4%.)

2%	4%	8%	10%	20%	50%	25%	100%
	20						
	30						
					60		
			50				

- **9.** a) If 45% is 9, what is 90%?
  - c) If 40% is 64, what is 100%?

- b) If 3% is 12, what is 1%?
- d) If 20% is 13, what is 100%?

**10.** Arti wants to leave a 15% tip on a meal that cost \$60. How much tip should she leave? (Hint: 15% = 10% + 5%.)

11. a) A shirt that usually costs \$40 is on sale for 25% off. What is 25% of \$40? What is \$40 – (25% of \$40)? What is the sale price of the shirt?

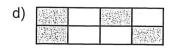
b) How would you estimate the price if a shirt that usually costs \$32.99 is on sale for 25% off?

### NS7-68 Visual Representations of Percents

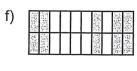
What percent of the figure is shaded?







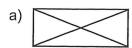




%



2. Shade 50% of the rectangle.



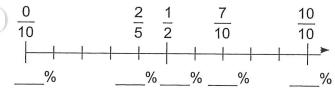


3. Write different expressions for the shaded area.

$$\frac{1}{20} = \frac{1}{100} = 0.$$



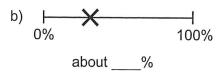
4. Write the percents that are equivalent to the fractions.



5. Measure the line segment. Extend the segment to show 100%.

**6.** Estimate the percent of the line segment to the left of the mark.





- 7. 20 m² of a 50 m² field is used for growing potatoes. What fraction and percent of the field is this?
- 8. David has run 4 km of a 20 km cross-country race. What fraction and percent of the race has he completed? What percent of the race is left to run?
  - When would you use the measurement to describe the amount, and when would you use the percent (if ever)? Write a sentence using each expression.
  - a) 3 h of the school day or 50% of the school day
- b) 12 kg of berries or 40% of the berries

# NS7-69 Comparing Fractions, Decimals, and Percents

Complete the chart

Fraction	$\frac{1}{4}$		$\frac{3}{20}$			6 15	23 25		
Decimal		0.35			0.60				0.55
Percent				40%				75%	

- 2. Write < or > or = between each pair of numbers. First change the numbers to a pair of decimal fractions with the same denominator.

- 53%

- c)  $\frac{1}{4}$  23% d)  $\frac{3}{4}$
- 70%

- $1 \times 50$

- 32%
- f) 0.27

- g) 0.02 11% h)  $\frac{1}{10}$
- 10%

- 93% j)  $\frac{23}{50}$  46% k) 0.9
- 10%
- 19%

- 3. Change the numbers in each set to decimals. Then order the decimals from least to greatest.
  - a)  $\frac{3}{5}$ , 42%, 0.73

b)  $\frac{1}{2}$ , 0.73, 80%

- c)  $\frac{1}{4}$ , 0.09, 15%
- a) In Abeed's school,  $\frac{3}{5}$  of students like gym and 65% like drama. Which class is more popular?
  - b) In Rachel's class, 0.45 of the students like pepperoni pizza best, 35% like cheese, and  $\frac{1}{5}$  like vegetarian. Which type of pizza do the most students like best?